

ι	$==:$	ι
1	$==:$	1
0	$==:$	0
$P\sim$	$==:$	$P\sim$
$P\cap Q$	$==:$	$P\cap Q$
$P\Delta Q$	$==:$	$P\Delta Q$
$P\circ Q$	$==:$	$P\circ Q$
\overline{P}	$==:$	$P\Delta 1$
δ	$==:$	$\bar{\iota}$
$P-Q$	$==:$	$P\cap\overline{Q}$
$P\cup Q$	$==:$	$\overline{P-Q}$

\emptyset	$==:$	0
$\mathbf{1}$	$==:$	1
$\text{rA}(P)$	$==:$	$P \circ \mathbf{1}$
$\text{lA}(P)$	$==:$	$\mathbf{1} \circ P$
$\text{diag}(P)$	$==:$	$P \cap \iota$
$\text{mult}(P)$	$==:$	$P \cap P \circ \delta$
$\text{dom}(P)$	$==:$	$\text{diag}(\text{rA}(P))$
$\text{img}(P)$	$==:$	$\text{diag}(\text{lA}(P))$
$\text{bros}(P, Q)$	$==:$	$P \overset{\sim}{\circ} Q$
$\text{bros}(P)$	$==:$	$\text{bros}(P, P)$
$\text{sibs}(P, Q)$	$==:$	$P \circ Q \overset{\sim}{}$
$\text{tot}(P)$	$==:$	$P \Delta (\iota - \text{rA}(P))$
$P \dagger Q$	$==:$	$\overline{P \circ Q}$
$\text{rR}(P, Q)$	$==:$	$\overline{\text{bros}(Q, \overline{P})}$
$\text{lR}(P, Q)$	$==:$	$\overline{\text{sibs}(\overline{P}, Q)}$
$\text{syq}(P, Q)$	$==:$	$\text{rR}(Q, P) \cap \text{rR}(\overline{Q}, \overline{P})$
$\text{noy}(P)$	$==:$	$\text{syq}(P, P)$
$\text{qNodes}(P)$	$==:$	$P \cup P \overset{\sim}{}$
$\text{nodes}(P)$	$==:$	$\text{dom}(\text{qNodes}(P))$
$\text{arcs}(P)$	$==:$	$P - \iota$
$\text{isolated}(P)$	$==:$	$\text{nodes}(P) - \text{nodes}(P - \iota)$
$\cap(\emptyset)$	$==:$	$\mathbf{1}$
$\cap([P])$	$==:$	P
$\cap([P, Q R])$	$==:$	$\cap([P \cap Q R])$
$\circ(\emptyset)$	$==:$	ι
$\circ([P])$	$==:$	P
$\circ([P, Q R])$	$==:$	$\circ([P \circ Q R])$
$-([P])$	$==:$	P
$-([P, Q R])$	$==:$	$-([P - Q R])$
$\cup(\emptyset)$	$==:$	\emptyset
$\cup([P Q])$	$==:$	$\overline{-(\overline{P} Q)}$
$\text{sibs}([P])$	$==:$	$\text{sibs}(P, P)$
$\text{sibs}([P, Q])$	$==:$	$\text{sibs}(P, Q)$
$\text{sibs}([P, Q, R S])$	$==:$	$\text{sibs}(P, Q) \cap \text{sibs}([R S])$

$P \subseteq Q$	\leftrightarrow :	$\emptyset_-(P, Q)$
$P \supseteq Q$	\leftrightarrow :	$Q \subseteq P$
$\text{Disj}(P, Q)$	\leftrightarrow :	$\emptyset_ \cap (P, Q)$
$\text{Tot}(P)$	\leftrightarrow :	$\mathbf{1}_rA(P)$
$\text{RAbs}(P)$	\leftrightarrow :	$\text{is_rA}(P)$
$\text{LAbs}(P)$	\leftrightarrow :	$\text{is_lA}(P)$
$\text{Coll}(P)$	\leftrightarrow :	$\text{is_diag}(P)$
$\text{RUniq}(P)$	\leftrightarrow :	$\emptyset_ \text{mult}(P)$
$\text{LUniq}(P)$	\leftrightarrow :	$\text{Coll}(\text{sibs}(P, P))$
$\text{RUniq}(P, Q)$	\leftrightarrow :	$\text{Disj}(\text{mult}(Q), \text{rA}(P))$
$\text{LUniq}(P, Q)$	\leftrightarrow :	$\text{RUniq}(P, Q^\sim)$
$\text{sends}(P, Q, R)$	\leftrightarrow :	$Q \circ P \subseteq \text{lA}(R)$
$\text{isSurj}(P, Q, R)$	\leftrightarrow :	$Q \subseteq \text{img}(R \circ P)$
$\text{isSurj}(P, Q)$	Θ :	[$\text{Coll}(Q),$ $Q \subseteq \text{lA}(P)$]
$\text{=}(P)$	Θ :	[$\text{true}(P)$]
$\text{=}(P, Q R)$	Θ :	[$P=Q$ $ \text{=}(P R)$]
$\subseteq(P)$	Θ :	[$\text{true}(P)$]
$\subseteq(P, Q R)$	Θ :	[$P \subseteq Q$ $ \subseteq(P R)$]
$\text{nameLets}()$	Θ :	[\square]
$\text{nameLets}(P, Q R)$	Θ :	[$P =: Q$ $ \text{nameLets}(R)$]
$\text{th}(P, - \text{one})$	\equiv :	P
$\text{th}(P, Q \text{incr}(R))$	\equiv :	$\text{th}(Q, Q, R) \circ P$
$\text{succth}(P, Q \text{decr}(R))$	\equiv :	$\text{th}(P, Q, R)$
$\text{tuples}(P Q)$	\equiv :	$\text{img}(P) \cap \text{dom}(\text{th}(P, P, Q)) - \text{dom}(\text{succth}(P, P, Q))$
$\text{sibs}(-, - \text{nil})$	\equiv :	$\mathbf{1}$
$\text{sibs}(P, Q \text{sng}(R))$	\equiv :	$\text{sibs}([\text{succth}(P, Q, R)])$
$\text{sibs}(P, Q \text{cons}(R, S))$	\equiv :	$\text{sibs}([\text{succth}(P, Q, R)]) \cap \text{sibs}(P, Q, S)$

$P=Q \& R=S$	\leftrightarrow :	$\emptyset \cup (P \Delta Q, R \Delta S)$
$\text{Boo}(P)$	\leftrightarrow :	$\text{LAbs}(P) \& \text{RAbs}(P)$
$\diamond P$	$=$:	$\text{rA}(\text{IA}(P))$
$\text{NonVoid}(P)$	\leftrightarrow :	$\mathbb{1} \cdot \diamond(P)$
$\neg P=Q$	\leftrightarrow :	$\mathbb{1} \cdot \diamond(P \Delta Q)$
$P \neq Q$	\leftrightarrow :	$\neg P=Q$
true	\leftrightarrow :	$\text{is}_\cdot(\iota)$
false	\leftrightarrow :	$\emptyset \cdot (\iota)$
$\text{link}(P, Q)$	$=$:	$\text{rA}(P) \circ Q$
$\text{Betw}(P, Q, R)$	\leftrightarrow :	$Q \subseteq \text{link}(P, R)$
$\text{Dngl}(P)$	\leftrightarrow :	$\text{Coll}(\text{link}(P, P))$
$P=Q \vee R=S$	\leftrightarrow :	$\emptyset \cdot \text{link}(P \Delta Q, R \Delta S)$
$P=Q \rightarrow R=S$	\leftrightarrow :	$\emptyset \cdot \circ(\diamond(P \Delta Q), R \Delta S)$
$\text{diff}(\llbracket \rrbracket)$	$=$:	\emptyset
$\text{diff}(\llbracket P=Q \rrbracket)$	$=$:	$P \Delta Q$
$\text{diff}(\llbracket P=Q, R=S \rrbracket T \rrbracket)$	$=$:	$P \Delta Q \cup \text{diff}(\llbracket R=S \rrbracket T \rrbracket)$
$\text{link}(\llbracket \rrbracket)$	$=$:	ι
$\text{link}(\llbracket P=Q \rrbracket)$	$=$:	$\text{link}(P, Q)$
$\text{link}(\llbracket P=Q, R=S \rrbracket T \rrbracket)$	$=$:	$\text{link}(\text{link}(P, Q), \text{link}(\llbracket R=S \rrbracket T \rrbracket))$
$\&(P)$	\leftrightarrow :	$\emptyset \cdot \text{diff}(P)$
$\vee(P)$	\leftrightarrow :	$\emptyset \cdot \text{link}(P)$
$\text{Sngl}(P)$	Θ :	[$\text{NonVoid}(P)$, $\text{RUniq}(\text{IA}(P))$, $\text{LUniq}(P)$]
$\text{isSngl}(P)$	\leftrightarrow :	$\&\text{-Sngl}(P)$
$\text{DotDot}(P, Q, R)$	Θ :	[$\text{Betw}(P, Q, R)$, $R \subseteq \text{IA}(Q)$, $P \subseteq \text{rA}(Q^\smile)$]
$\text{DotDDot}(P, Q, R)$	\leftrightarrow :	$\&\text{-DotDot}(P, Q, R)$
$\text{Dotdot}(P, Q, R)$	\leftrightarrow :	$\&([\text{Betw}(P, Q, R), \text{isSurj}(Q, R, P), \text{isSurj}(Q^\smile, P, R)])$
$\text{Const}(P)$	Θ :	[$\text{Dngl}(P)$, $\text{NonVoid}(P)$]
$\text{Point}(P)$	Θ :	[$\text{RAbs}(P)$, $\text{LUniq}(P)$, $\text{NonVoid}(P)$]
$\text{Skolem}(P, Q, R)$	Θ :	[$R =: Q$, $R \subseteq P$, $\text{RUniq}(R)$, $\text{rA}(R) = \text{rA}(P)$]

-- Five ways of stating that the universe of discourse is singleton

CardUniv1 $\leftrightarrow: \emptyset_{\cdot o}(\bar{\iota}, \bar{\iota})$

CardUniv1B $\leftrightarrow: \mathbb{1}_{\cdot \iota}$

CardUniv1C $\leftrightarrow: \text{is}_{\cdot o}(\bar{\iota}, \bar{\iota})$

CardUniv1D $\leftrightarrow: \emptyset_{\cdot o}(\mathbb{1}, \bar{\iota})$

CardUniv1E $\leftrightarrow: \emptyset_{\cdot o}(\bar{\iota}, \mathbb{1})$

-- One way of stating that the universe of discourse is at least doubleton

CardUnivGt1 $\leftrightarrow: \mathbb{1}_{\cdot o}(\mathbb{1}, \bar{\iota})$

-- One way of stating that the universe of discourse is doubleton

CardUniv2 $\leftrightarrow: \iota_{\cdot o}(\bar{\iota}, \bar{\iota})$

-- One way of stating that the universe of discourse is more than doubleton

CardUnivGt2 $\leftrightarrow: \mathbb{1}_{\cdot o}(\bar{\iota}, \bar{\iota})$

isTrans(P) $\leftrightarrow: P \circ P \subseteq P$

isSymm(P) $\leftrightarrow: \text{is}_{\cdot \sim}(P)$

isRefl(P) $\leftrightarrow: P \cup P^{\sim} \subseteq \text{rA}(\iota \cap P)$

isStrict(P) $\leftrightarrow: \emptyset_{\cdot \text{diag}}(P)$

isAntisymm(P) $\leftrightarrow: P \cap P^{\sim} \subseteq \iota$

isTrich(P) $\leftrightarrow: \mathbb{1}_{\cdot \cup}([P, \iota, P^{\sim}])$

isAsymm(P) $\leftrightarrow: \emptyset_{\cdot \cap}(P, P^{\sim})$

isTotRefl(P) $\leftrightarrow: \iota \subseteq P$

isConnex(P) $\leftrightarrow: \mathbb{1}_{\cdot \cup}(P, P^{\sim})$

isPreord(P) $\Theta: [$
 isRefl(P),
 isTrans(P)
 $]$

isEquiv(P) $\Theta: [$
 isSymm(P),
 isTrans(P)
 $]$

isFunc(P) $\leftrightarrow: \text{bros}(P) \subseteq \iota$

isEquiv(P, Q) $\Theta: [$
 isFunc(Q),
 is $_{\cdot o}(Q, Q)$,
 $Q \circ Q^{\sim} = P$
 $]$

isGaloisCorr(P) $\Theta: [$
 $P \circ P \subseteq \iota$,
 isStrict(P),
 $P^{\sim} \subseteq \text{rA}(P)$
 $]$

isDense(P) $\leftrightarrow: \text{arcs}(P) \subseteq \text{arcs}(P) \circ \text{arcs}(P)$

isWithoutEndPoints(P) $\leftrightarrow: \iota \subseteq \text{link}(\text{arcs}(P), \text{arcs}^{\sim}(P))$

isNDMonotonic(P, Q) $\leftrightarrow: \emptyset_{\cdot \cap}(Q \circ P, P \circ Q)$

isBisim(P, Q) $\leftrightarrow: \emptyset_{\cdot \cup}(\text{IA}(P - P^{\sim}), Q \circ P - P \circ Q)$

$\text{areQProj}(P, Q, R, S)$	$\Theta:$	$[-, \rightarrow, \iota, \iota[$ $\text{isFunc}(P),$ $\text{isFunc}(Q),$ $\text{link}(R, S) \subseteq \text{bros}(P, Q)]$
$\text{areProj}(P, Q, R, S)$	$\Theta:$	$[-, \rightarrow, \iota, \iota[$ $\text{areQProj}(P, Q, R, S),$ $\text{Coll}(\text{sibs}([P, P, Q])),$ $\text{rA}(P) = \text{rA}(Q)]$
$\text{areQProj}(P, Q)$	$\Theta:$	$\text{areQProj}(P, Q, \rightarrow, -)$
$\text{areProj}(P, Q)$	$\Theta:$	$\text{areProj}(P, Q, \rightarrow, -)$
$\text{HdTIPure}(P, Q, R)$	$\Theta:$	$[$ $\text{areProj}(P, Q),$ $\text{Const}(R),$ $\text{rA}(P) = \text{rA}(\iota - R)]$
$\text{HdTI}(P, Q, R, S)$	$\Theta:$	$[$ $\text{areProj}(P, Q, R, \iota - R),$ $\text{Coll}(R),$ $\text{Const}(S),$ $\text{Disj}(S, R),$ $\text{Disj}(R, \text{IA}(Q)),$ $\text{rA}(P) = \overline{\text{rA}}(S \cup R)]$
$\text{HdTIFlat}(P, Q, R, S, T)$	$\Theta:$	$[\emptyset[$ $P \subseteq S,$ $\text{HdTI}(Q, R, S, T),$ $\text{NonVoid}(S),$ $\text{IA}(Q) = \text{IA}(S)]$
$\text{mXpr}(P, Q \parallel \text{atm}(R, S, T))$	$=:$	$\text{rA}(\text{th}(P, Q, S) \circ R \cap \text{th}(P, Q, T))$
$\text{mXpr}(P, Q \parallel \neg R)$	$=:$	$\overline{\text{mXpr}}(P, Q, R)$
$\text{mXpr}(P, Q \parallel R \& S)$	$=:$	$\text{mXpr}(P, Q, R) \cap \text{mXpr}(P, Q, S)$
$\text{mXpr}(P, Q \parallel R \oplus S)$	$=:$	$\text{mXpr}(P, Q, R) \Delta \text{mXpr}(P, Q, S)$
$\text{mXpr}(P, Q \parallel \exists(R, S))$	$=:$	$\text{sibs}(P, Q, S) \circ \text{mXpr}(P, Q, R)$
$\text{Maddux}(P, Q, R)$	$\Theta:$	$[$ $R(S) \leftrightarrow: \text{mXpr}(P, Q, S) = \mathbb{1}]$
$\text{areTotQProj}(P, Q, R)$	$\Theta:$	$[$ $\text{areQProj}(P, Q),$ $\text{Tot}(P),$ $\text{Tot}(Q),$ $R(S) \leftrightarrow: \text{mXpr}(P, Q, S) = \mathbb{1}]$

$\text{graphIsom}(P, Q, R)$	$\Theta:$ [$\text{bros}(Q) \subseteq \iota,$ $\text{sibs}(Q, Q) \subseteq \iota,$ $\text{dom}(Q) = \text{nodes}(P),$ $\text{img}(Q) = \text{nodes}(R),$ $P = Q \circ R \circ Q^{-1}$
$\text{graphIsom}(P, Q, R, S, T, W)$	$\Theta:$ [$\text{nameLets}([S, P, W, R, T, Q]),$ $\text{nodes}(P) =: \text{dom}(P \cup P^{-1}),$ $\text{graphIsom}(S, T, W)$
$\text{Maps}(P, Q, R)$	$\Theta:$ [$\text{Coll}(Q),$ $\text{Coll}(R),$ $Q \circ P \subseteq \text{IA}(R)$
$\text{Exhs}(P, Q, R)$	$\Theta:$ [$[\rightarrow, \rightarrow, \iota]$ $\text{Coll}(R),$ $\text{Coll}(Q),$ $Q \subseteq \text{IA}(R) \circ P$
$\text{Disj}(P, Q, R)$	$\Theta:$ [$[\rightarrow, \rightarrow, \iota]$ $\text{Coll}(Q),$ $\text{Coll}(R),$ $P \circ R \circ P^{-1} \cap \text{link}(Q, Q) \subseteq \iota$
$\text{Splits}(P, Q, R)$	$\Theta:$ [$\text{Exhs}(P, R, Q),$ $\text{Disj}(P, Q, R)$
$\text{IndClosed}(P, Q, R)$	$\Theta:$ [$R \subseteq P,$ $\text{Maps}(Q, P, P - R),$ $[\text{Coll}(S), R \subseteq S, S \circ Q \subseteq \text{IA}(S)] \Rightarrow P \subseteq S$
$\text{Sends}(P, Q, R)$	$\Theta:$ [$\text{RUniq}(P),$ $\text{Maps}(P, Q, R)$
$\text{Surj}(P, Q, R)$	$\Theta:$ [$[\rightarrow, \rightarrow, \iota]$ $\text{RUniq}(P),$ $\text{Exhs}(P, Q, R)$
$\text{Inj}(P, Q, R)$	$\Theta:$ [$[\rightarrow, \rightarrow, \iota]$ $\text{RUniq}(P),$ $\text{Disj}(P, Q, R)$
$\text{Bij}(P, Q, R)$	$\Theta:$ [$\text{RUniq}(P),$ $\text{Splits}(P, Q, R)$
$\text{SuccClosed}(P, Q, R)$	$\Theta:$ [$\text{RUniq}(Q),$ $\text{IndClosed}(P, Q, R)$

oppRevFp(P)	==:	$P \cap \bar{t} \circ P$
double(\square)	==:	\emptyset
double($[P Q]$)	==:	$\cup(\{\text{oppRevFp}(P), \text{oppRevFp}(P^\sim), \text{double}(Q)\})$
together($[P Q]$)	==:	$\text{arcs}(P) \cup \text{rA}(P) \cap (\text{double}(Q) \cup \text{IA}(P) \cap \cup(Q))$
inBoth($[P]$)	==:	$\text{rA}(P) \cap \text{rA}(P^\sim)$
inBoth($[P, Q R]$)	==:	$\cup(\{\text{rA}(P) \cap \text{rA}(Q), \text{rA}(P) \cap \text{rA}(Q^\sim), \text{rA}(P^\sim) \cap \text{rA}(Q), \text{inBoth}([P R]), \text{inBoth}([Q R])\})$
twice(\square)	==:	\emptyset
twice($[P Q]$)	==:	$\cup(\{\text{rA}(\text{mult}(P)), \text{rA}(\text{mult}(P^\sim)), \text{inBoth}([P Q]), \text{twice}(Q)\})$
Placeholders($[P Q]$)	↔:	$\emptyset \cup (\text{together}([P Q]), P \cap \text{twice}(Q))$

$\text{flagDom}(_ \text{zero})$	$=:$	$\mathbf{1}$
$\text{flagDom}(P \text{one})$	$=:$	$\text{dom}(P)$
$\text{Attr}(P, Q, R, S)$	$\Theta:$	[$\text{RUniq}(P),$ $\text{dom}(P) \subseteq Q,$ $\text{img}(P) \subseteq R,$ $Q \subseteq \text{flagDom}(P, S)$
$\text{keyPIH}(_)$	$=:$	\emptyset
$\text{keyPIH}([P, Q R])$	$=:$	$P \cap \text{img}(Q) \cup \text{keyPIH}([P R])$
$\text{isKeyPIH}(P)$	$\leftrightarrow:$	$\emptyset_ \text{keyPIH}(P)$
$\text{KeyPIH}([P])$	$\Theta:$	$\text{Coll}(P)$
$\text{KeyPIH}([P, Q R])$	$\Theta:$	[$\emptyset_ \cap (P, \text{img}(Q))$ $ \text{KeyPIH}([P R])$
$\text{keyFunc}([P], Q, R S)$	$=:$	$\text{succth}(Q, R, S) \circ P^\sim$
$\text{keyFunc}([P, Q R], S, T \text{decr}(W))$	$=:$	$\text{th}(S, T, W) \circ P^\sim \cap \text{keyFunc}([Q R], S, T, W)$
$\text{Key}([P, Q, R S])$	$\Theta:$	[$\text{RUniq}(\text{keyFunc}(S, Q, R, 0))$ $ \text{KeyPIH}([P S])$
$\text{IBoth}(P, Q)$	$=:$	$\text{rA}(P) \cap \text{rA}(Q)$
$\text{NoLLBoth}(P, Q, R)$	$\leftrightarrow:$	$\emptyset_ \cap (\text{IBoth}(Q, R), P)$
$\text{NoLRBoth}(P, Q, R)$	$\leftrightarrow:$	$\text{NoLLBoth}(P, Q, R^\sim)$
$\text{NoTogether}(P, Q)$	$\leftrightarrow:$	$\emptyset_ \cap (\text{rA}(P) \cap \text{IA}(P), Q)$
$\text{RXcl}(P, Q)$	$\leftrightarrow:$	$\emptyset_ \cap (\text{mult}(Q), \text{IA}(P))$
$\text{LXcl}(P, Q)$	$\leftrightarrow:$	$\text{RXcl}(P, Q^\sim)$
$\text{NoTwice}([P])$	$\Theta:$	$\text{true}(P)$
$\text{NoTwice}([P, Q R])$	$\Theta:$	[$\text{RUniq}(P, Q),$ $\text{LUniq}(P, Q),$ $\text{NoTogether}(P, Q),$ $\text{RXcl}(P, Q),$ $\text{LXcl}(P, Q)$ $ \text{NoTwice}([P R])$
$\text{NoLRBoth}([P, Q])$	$\Theta:$	$\text{true}([P, Q])$
$\text{NoLRBoth}([P, Q, R S])$	$\Theta:$	[$\text{NoLLBoth}(P, Q, R),$ $\text{NoLRBoth}(P, Q, R),$ $\text{NoLRBoth}(P, R, Q)$ $ \text{NoLRBoth}([P, Q S])$
$\text{NoBoth}([P])$	$\Theta:$	$\text{true}(P)$
$\text{NoBoth}([P, Q R])$	$\Theta:$	[$\text{NoLRBoth}(P, Q, Q)$ $ \{\text{NoLRBoth}([P, Q R]), \text{NoBoth}([P R])\}$
$\text{PlaceHolders}([P, Q R])$	$\Theta:$	$\{\text{NoTwice}([P, Q R]), \text{NoBoth}([P, Q R])\}$
$\text{Entity}(P, Q)$	$\Theta:$	[$\text{Coll}(Q),$ $\text{Disj}(Q, P)$
$\text{IsA}([P, Q, R])$	$\Theta:$	[ℓ [$R \subseteq P,$ $\text{Disj}(R, Q)$
$\text{IsA}([P, Q, R, S T])$	$\Theta:$	[ℓ [$R \subseteq S$ $ \text{IsA}([P, Q, S T])$
$\text{DotDot}(P, Q, R, S)$	$\Theta:$	[$\text{Betw}(Q \Delta P, R, S \Delta P),$ $S \subseteq \text{IA}(R),$

