

$\text{semiGroup}(P)$	$\Theta:$	[$P(P(Q, R), S)=P(Q, P(R, S))]$
			-- : associative law
$\text{leftMonoid}(P, Q)$	$\Theta:$	[$\text{semiGroup}(P),$ $P(Q, R)=R]$
			-- : left monoid
$\text{rightMonoid}(P, Q)$	$\Theta:$	[$\text{semiGroup}(P),$ $P(R, Q)=R]$
			-- : right monoid
$\text{monoid}(P, Q)$	$\Theta:$	[$\text{leftMonoid}(P, Q),$ $P(R, Q)=R]$
			-- : bilateral monoid
$\text{commMonoid}(P, Q)$	$\Theta:$	[$\text{leftMonoid}(P, Q),$ $P(R, S)=P(S, R)]$
			-- : commutative monoid
$\text{leftDistributes}(P, Q)$	$\Theta:$	[$P(R, Q(S, T))=Q(P(R, S), P(R, T))]$
			-- : left distributive law
$\text{rightDistributes}(P, Q)$	$\Theta:$	[$P(Q(R, S), T)=Q(P(R, T), P(S, T))]$
			-- : right distributive law
			$\text{semiGroup}(\Delta)$
			$\text{leftMonoid}(\circ, \iota)$
			$\text{commMonoid}(\cap, \mathbb{1})$
			$(P\Delta Q)\circ R \subseteq Q\circ R \cup P\circ R$
			$[P \subseteq Q] \Rightarrow P\circ R \subseteq Q\circ R$
			$P \cap (Q\Delta R) \Delta P \cap Q = P \cap R$
			$P^{\sim\sim}=P$
			$(P \cap Q)^{\sim}=Q^{\sim} \cap P^{\sim}$
			$(P \circ Q)^{\sim}=Q^{\sim} \circ P^{\sim}$
			$[P \circ Q \cap R = \emptyset] \Rightarrow P^{\sim} \circ R \cap Q = \emptyset$