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-- ----- PROOF -----
-- Length of proof is 22 . Level of proof is 10 .
-- 1 [ ]  $\neg x \subseteq y \vee x \cup y = y$ 
-- 2 [ ]  $x \subseteq y \vee x \cup y \neq y$ 
-- 5 [ ]  $\neg x \subseteq y \vee \neg x \subseteq z \vee x \subseteq y \cap z$ 
-- 6 [ ]  $x \cup y \neq y \vee z \circ x \cup z \circ y = z \circ y$ 
-- 7 [ ]  $x \cup y \neq y \vee \overline{z \cup y} \cup \overline{x} = \overline{x}$ 
-- 8 [ ]  $x \cup y \neq y \vee x \circ z \cup y \circ z = y \circ z$ 
-- 9 [ ]  $\neg (c4 \cap c2) \circ (c3 \cap c1) \subseteq c4 \circ c3$ 
-- 11 [ ]  $x \cup y = y \cup x$ 
-- 12 [ ]  $x \cup (y \cup z) = x \cup y \cup z$ 
-- 13 [ copy , 12 , flip . 1 ]  $x \cup y \cup z = x \cup (y \cup z)$ 
-- 17 [ ]  $x \cap y = \overline{\overline{x \cup y}}$ 
-- 18 [ copy , 17 , flip . 1 ]  $\overline{\overline{x \cup y}} = x \cap y$ 
-- 20 [ ]  $x \cup x = x$ 
-- 22 [ ]  $x \cap y \subseteq x$ 
-- 26 [ hyper , 20 , 7 ]  $\overline{\overline{x \cup y \cup y}} = \overline{y}$ 
-- 28 [ hyper , 20 , 2 ]  $x \subseteq x$ 

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-- 29 [ hyper , 28 , 5 , 28 ]  $x \subseteq x \cap x$ 
-- 33 [ hyper , 22 , 1 ]  $x \cap y \cup x = x$ 
-- 46 [ para_into , 11 . 1 . 1 , 1 . 2 . 1 , flip . 1 ]  $x \cup y = x \vee \neg y \subseteq x$ 
-- 62 [ hyper , 29 , 1 ]  $x \cup x \cap x = x \cap x$ 
-- 75 [ hyper , 33 , 8 ]  $(x \cap y) \circ z \cup x \circ z = x \circ z$ 
-- 79 [ hyper , 33 , 6 ]  $x \circ (y \cap z) \cup x \circ y = x \circ y$ 
-- 86 , 85 [ para_into , 33 . 1 . 1 , 11 . 1 . 1 ]  $x \cup x \cap y = x$ 
-- 88 , 87 [ back_demod , 62 , demod , 86 , flip . 1 ]  $x \cap x = x$ 
-- 176 , 175 [ para_into , 18 . 1 . 1 . 1 , 20 . 1 . 1 , demod , 88 ]  $\bar{\bar{x}} = x$ 
-- 249 [ hyper , 26 , 2 ]  $\overline{x \cup y} \subseteq \bar{y}$ 
-- 267 [ para_into , 249 . 1 . 1 . 1 , 11 . 1 . 1 ]  $\overline{x \cup y} \subseteq \bar{x}$ 
-- 274 [ para_into , 267 . 1 . 1 . 1 , 26 . 1 . 1 , demod , 176 , 176 ]  $x \subseteq y \cup x$ 
-- 293 [ para_into , 274 . 1 . 2 , 13 . 1 . 1 ]  $x \subseteq y \cup (z \cup x)$ 
-- 343 [ para_into , 293 . 1 . 2 . 2 , 46 . 1 . 1 ]  $x \subseteq y \cup z \vee \neg x \subseteq z$ 
-- 744 [ para_into , 343 . 1 . 2 , 46 . 1 . 1 ]  $x \subseteq y \vee \neg x \subseteq z \vee \neg z \subseteq y$ 
-- 2350 [ hyper , 75 , 2 ]  $(x \cap y) \circ z \subseteq x \circ z$ 
-- 2570 [ hyper , 79 , 2 ]  $x \circ (y \cap z) \subseteq x \circ y$ 
-- 6861 [ hyper , 2570 , 744 , 2350 ]  $(x \cap y) \circ (z \cap u) \subseteq x \circ z$ 
-- 6862 [ binary , 6861 . 1 , 9 . 1 ]  $F$ 

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--      end of proof      --
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-- Search stopped by max_proofs option .
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-- = = = = = end of search = = = = =
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--      statistics      --
-- clauses given 185
-- clauses generated 24739
-- clauses kept 6339
-- clauses forward subsumed 11909
-- clauses back subsumed 67
-- Kbytes malloced 4119
--
--      times ( seconds )      --
-- user CPU time 4 . 30 ( 0 hr , 0 min , 4 sec )
-- system CPU time 0 . 0 ( 0 hr , 0 min , 0 sec )
-- wall - clock time 5 ( 0 hr , 0 min , 5 sec )
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